



# ***Gravitational Waves***

Wind Crest Learners  
Academy for Lifelong Learning

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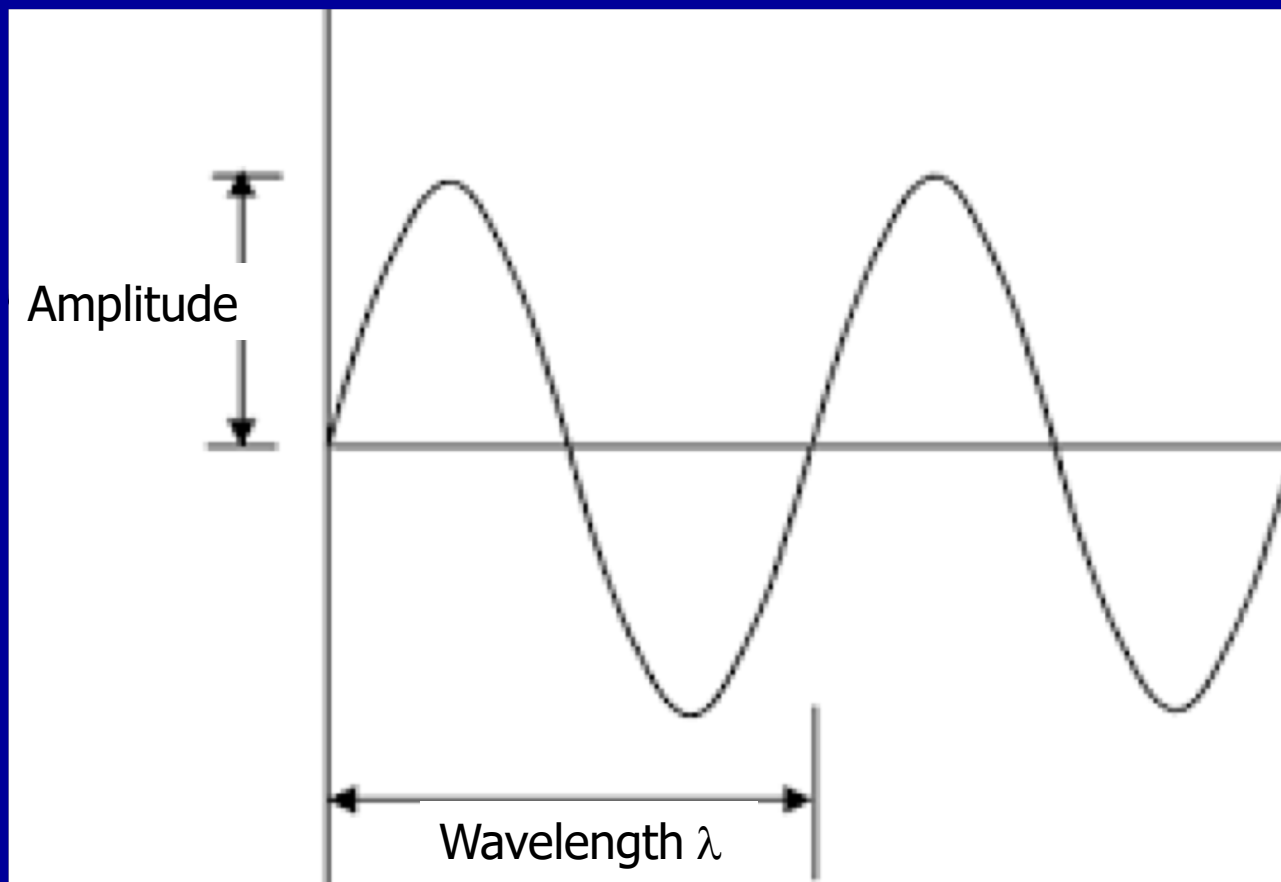
University of Denver

Department of Physics and Astronomy

# Electromagnetic waves

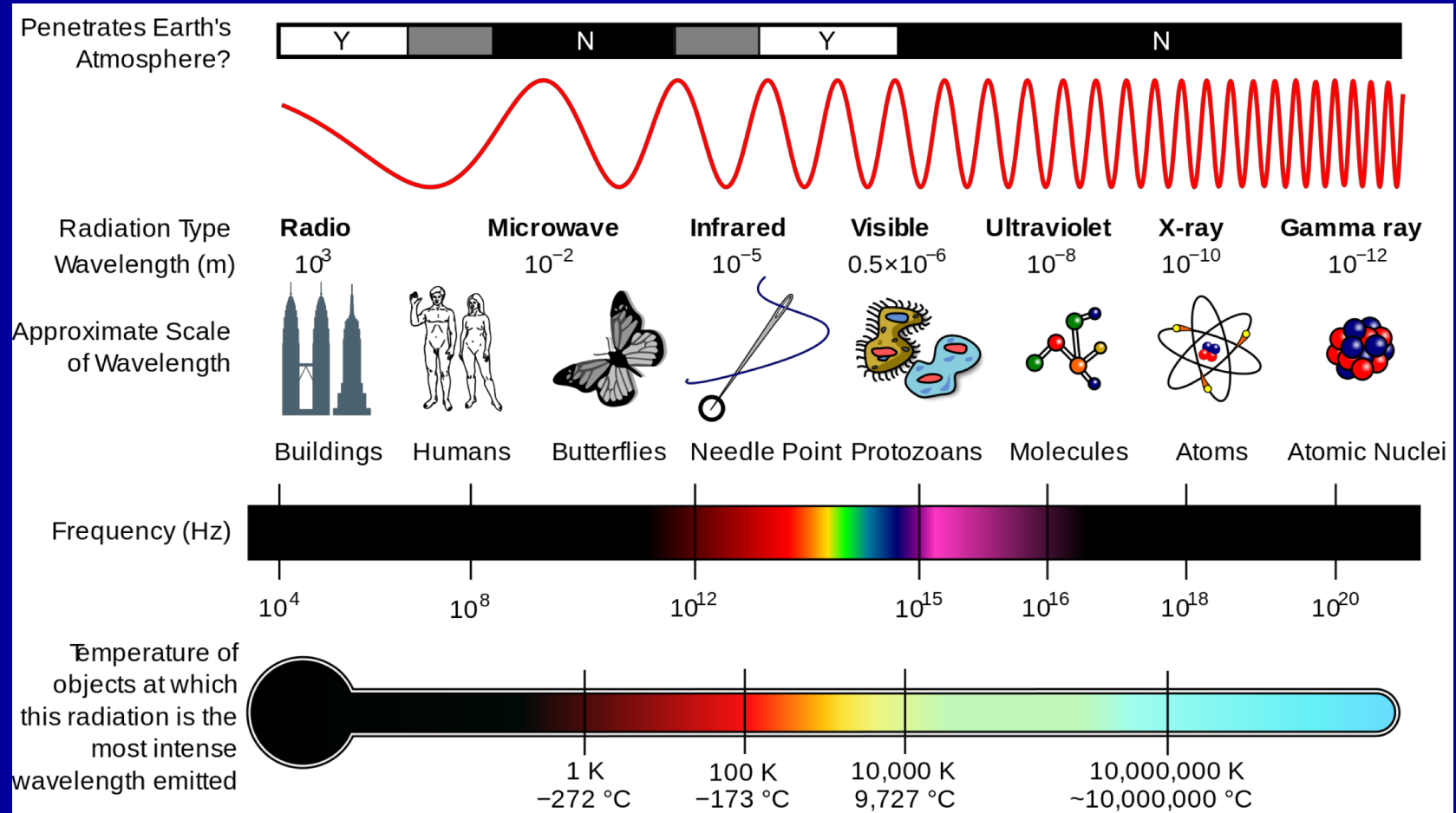
$$f=c/\lambda$$

Frequency is measured in cycles per second, a unit we call Hertz or symbolize Hz.

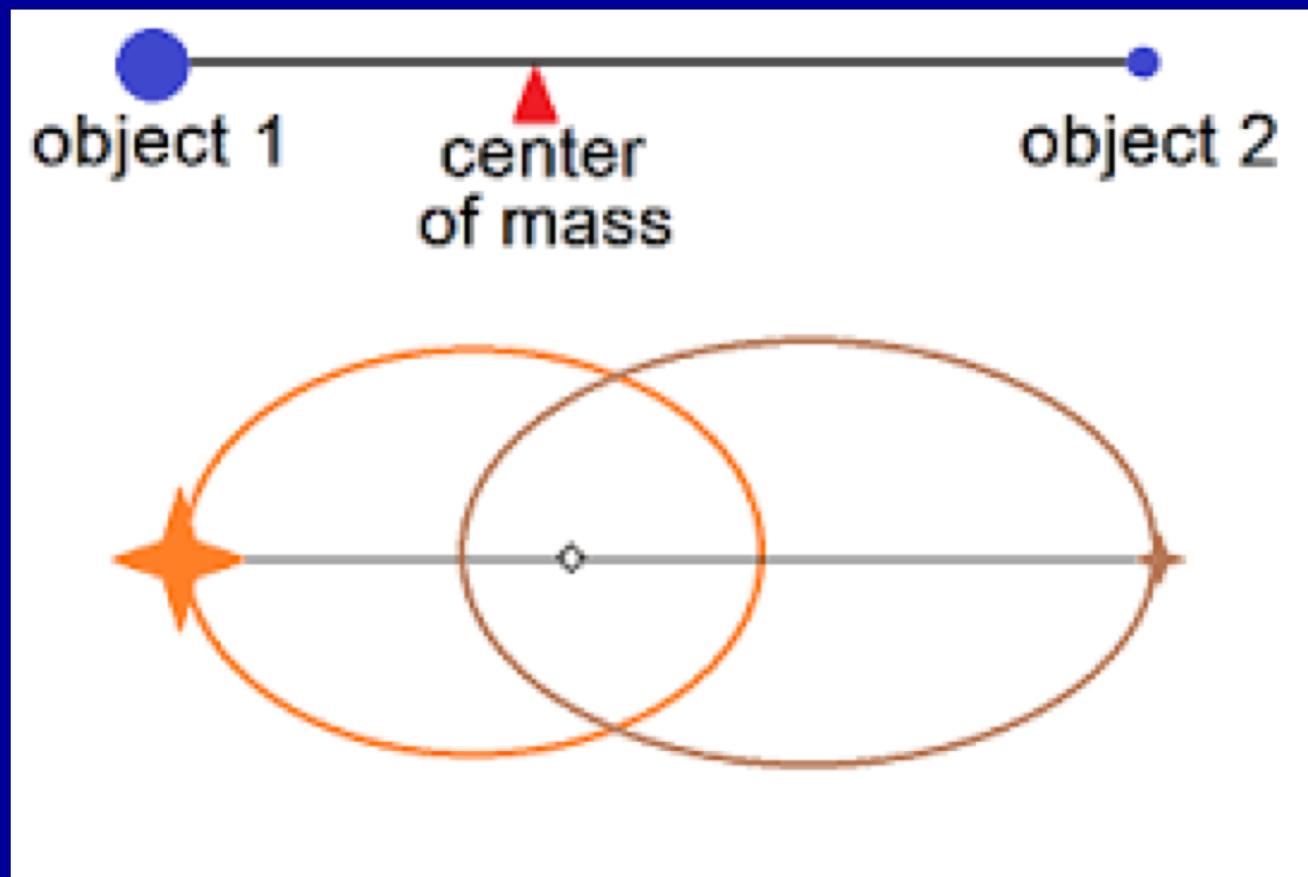


As wavelength gets longer (bigger), cycles per second gets slower (frequency decreases).

# The electromagnetic spectrum



# Binary orbits

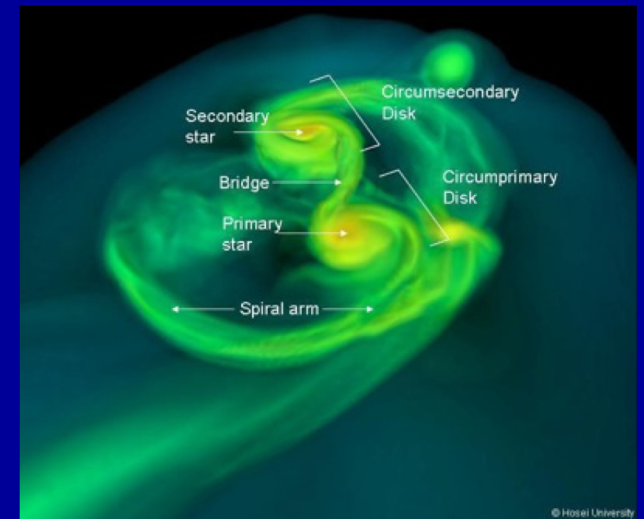
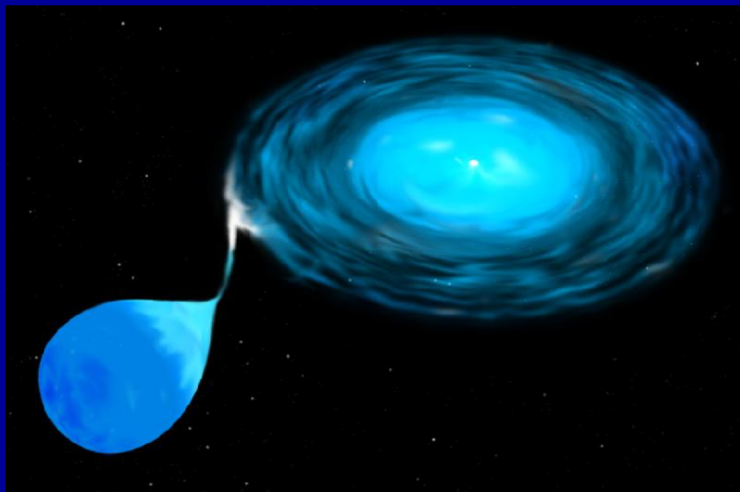


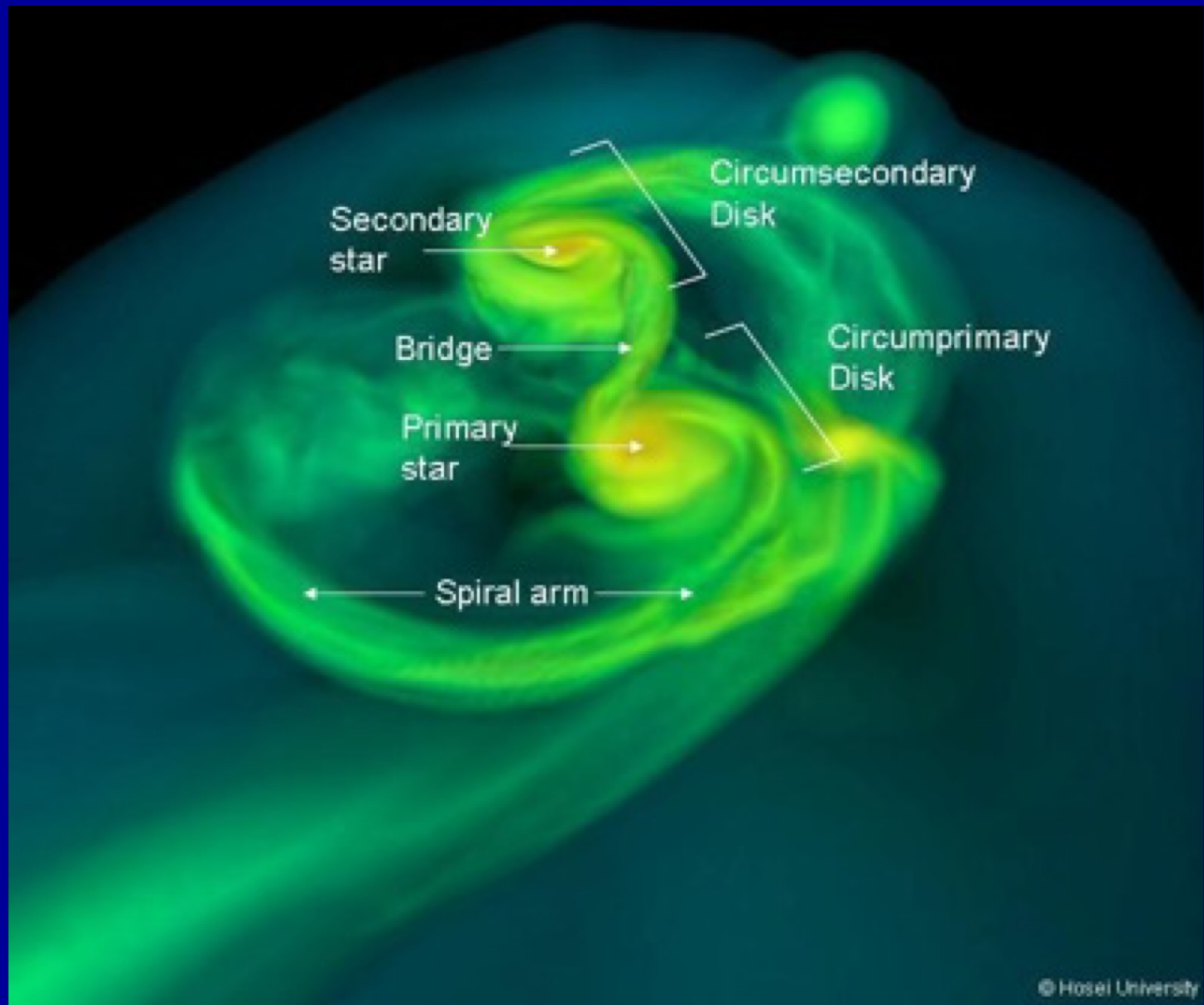


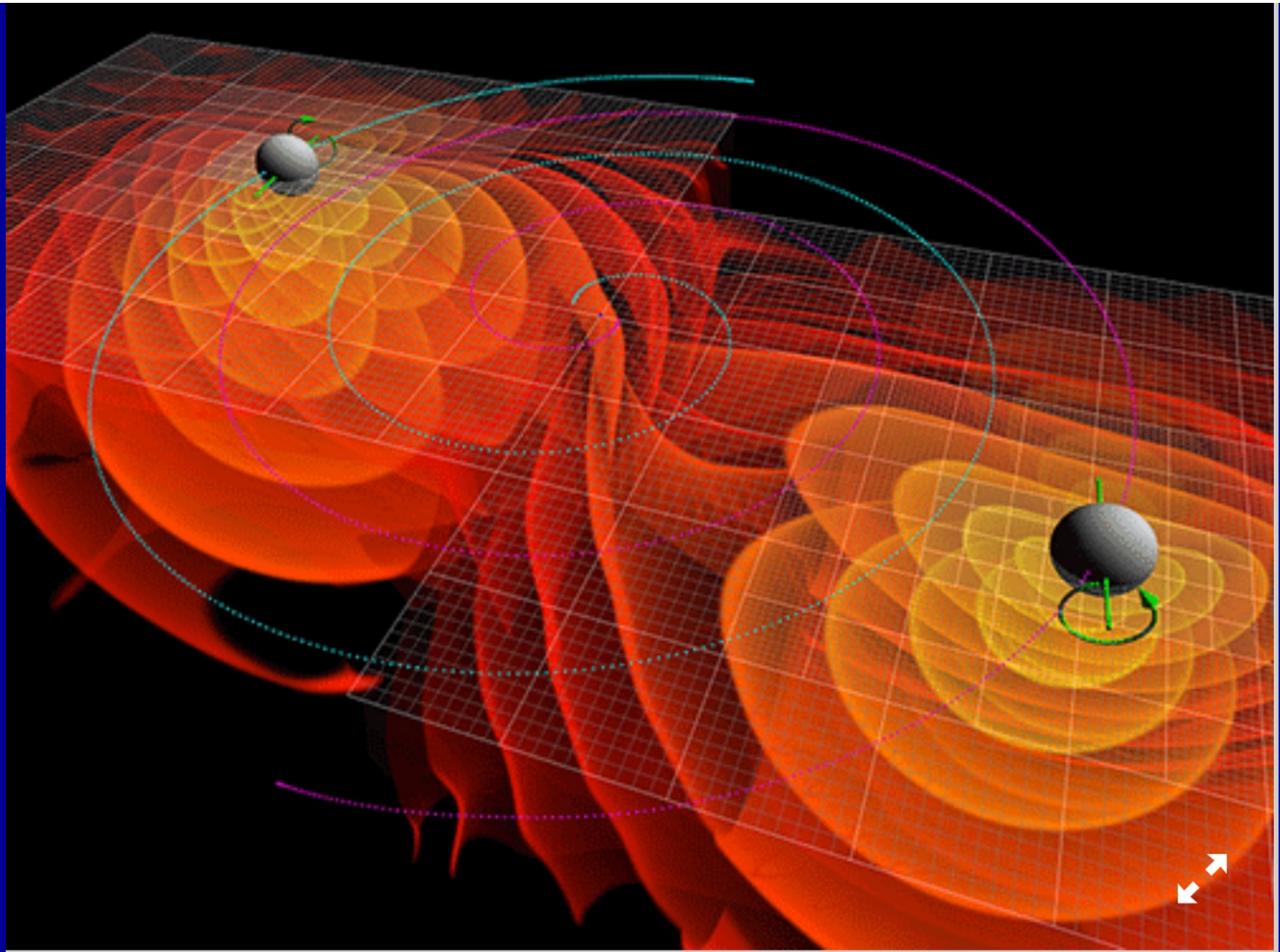
# Collapsed objects

- $0.6 < M_0 < 1.4$   $\Rightarrow$  white dwarf
- $1.1 < M_0 < 3.3$   $\Rightarrow$  neutron star (pulsars)
- $3.8 < M_0 < 10^9$   $\Rightarrow$  black hole

Many stars end up in binary systems, and one or both of the stars can collapse once its internal fuel is burned up.

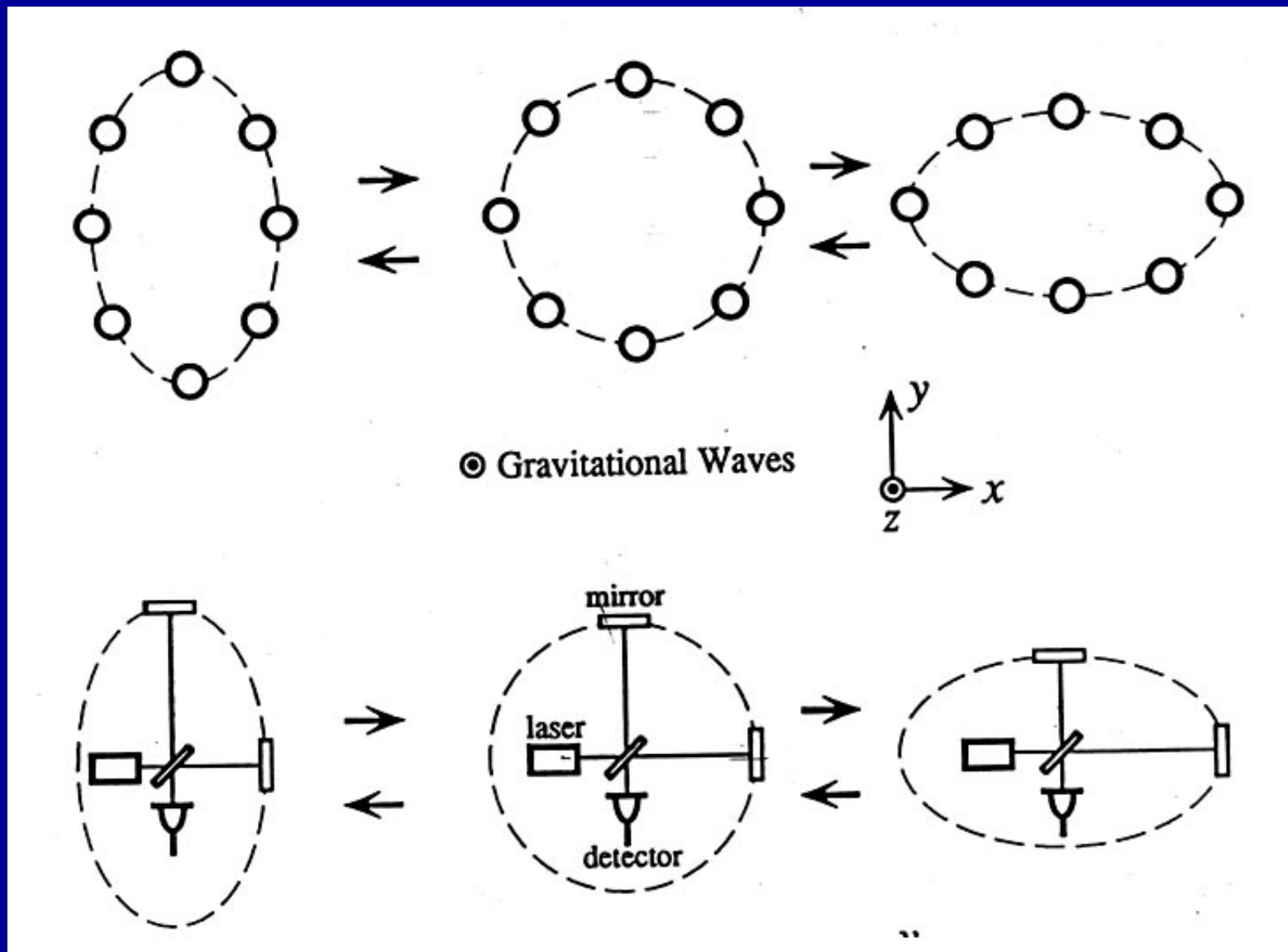






C. Henze/NASA Ames Research Center

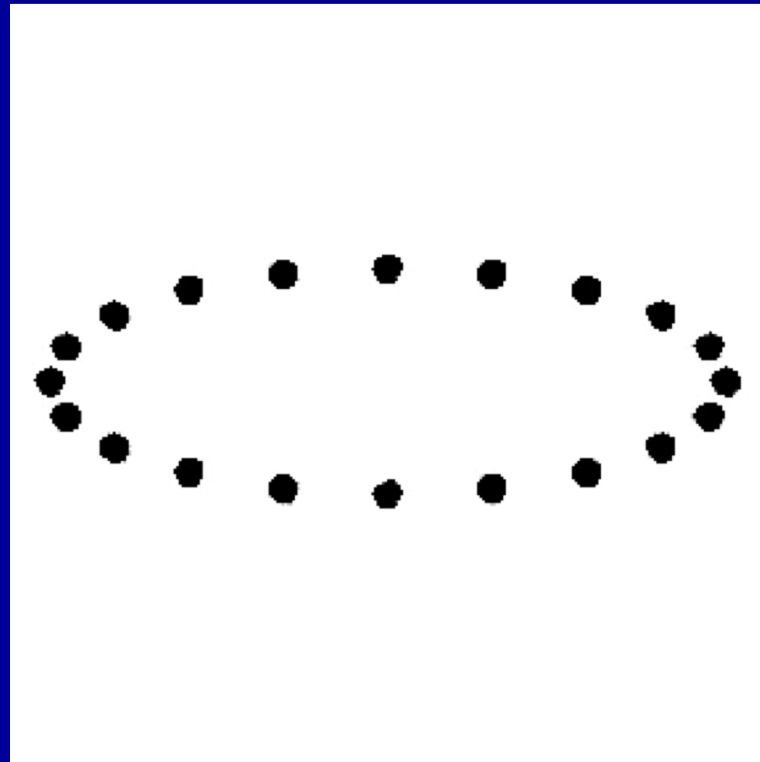




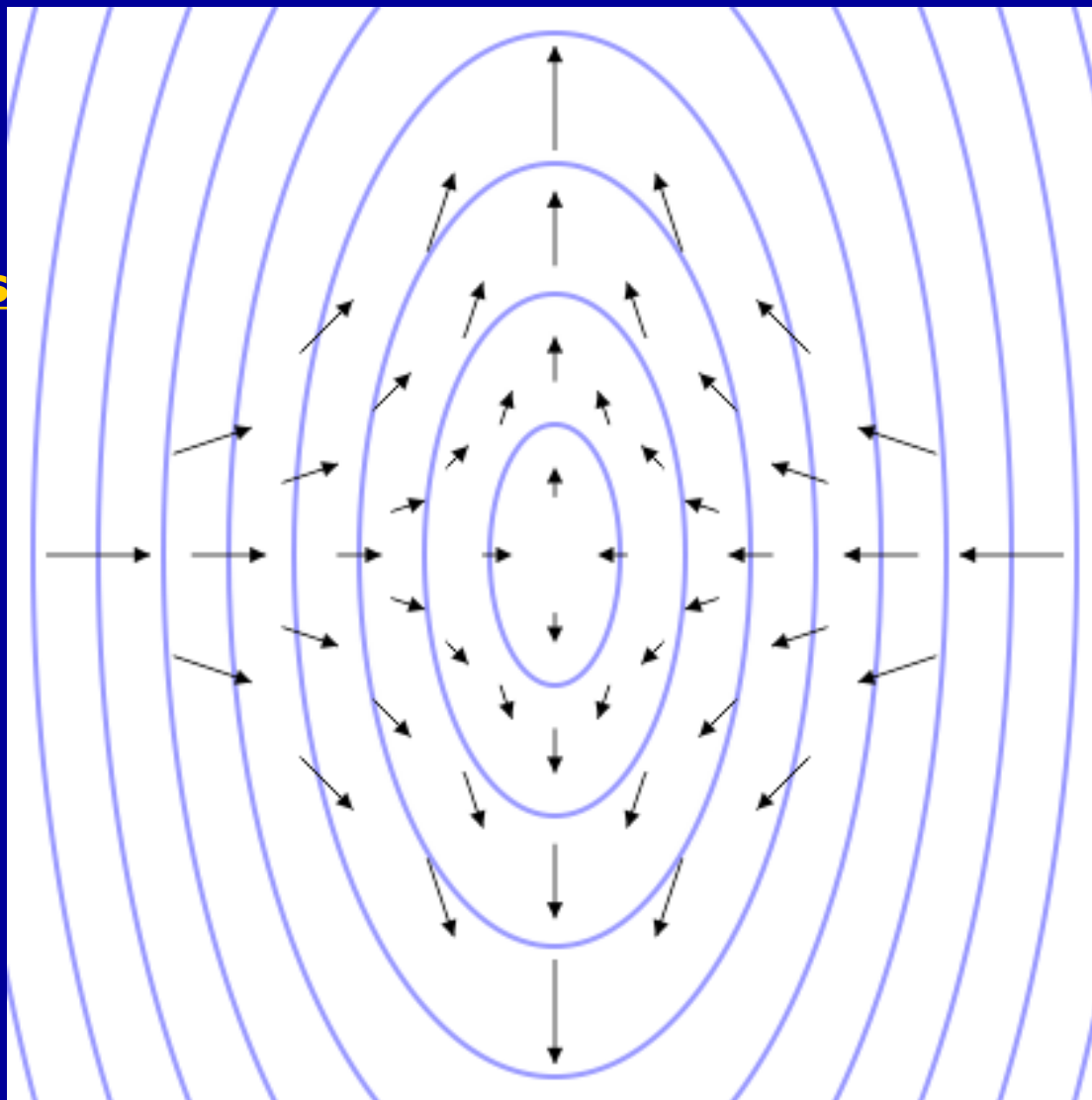
*graphic courtesy of B. Barish, LIGO-Caltech*  
*hula hoop courtesy of Craig and Arlene's grandchildren*

# Quadrupole wave

[https://en.wikipedia.org/wiki/File:Quadrupol\\_Wave.gif](https://en.wikipedia.org/wiki/File:Quadrupol_Wave.gif)

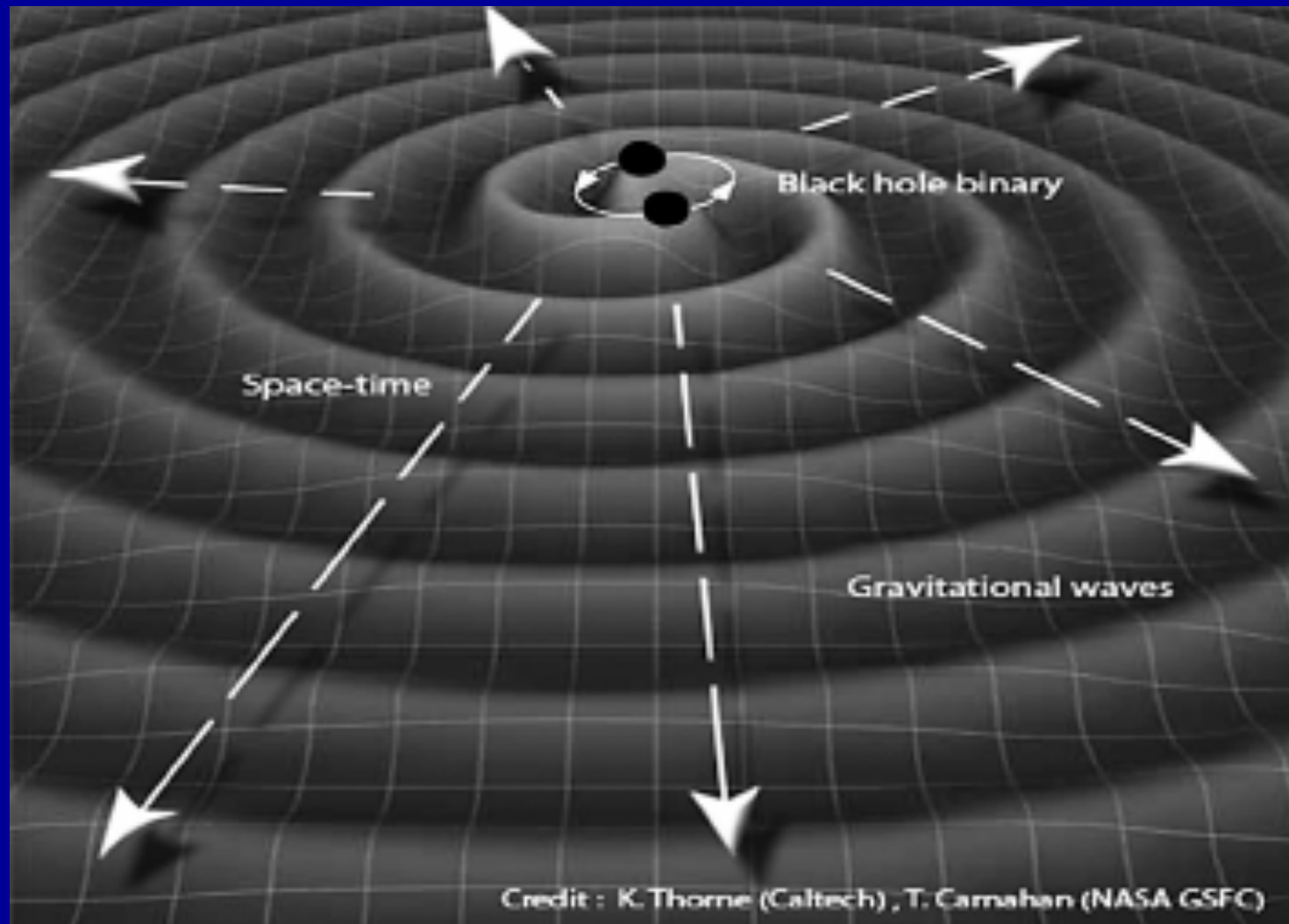


https



**ve.gif**

# Black Hole merger



# Pulse timing is important





# LIGO, late 1990s (first funding 1995)

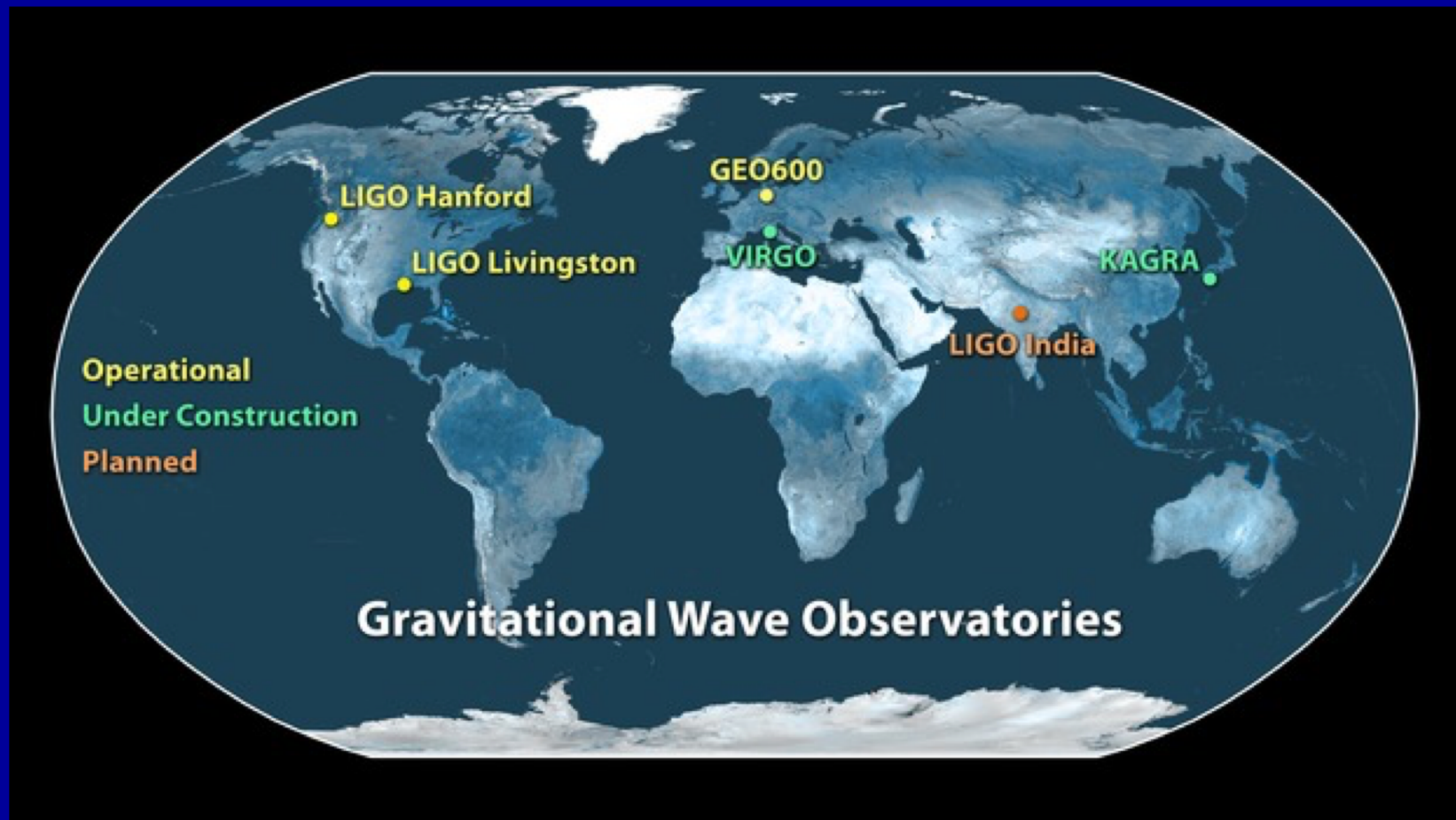
Arms 4 km long, masses 40 kg, basically mirrors. Motion detected  $10^{-19}$  m (aLIGO).



# Coincidence by aLIGO: Hanford, Washington and Livingston, Louisiana, (Italy)

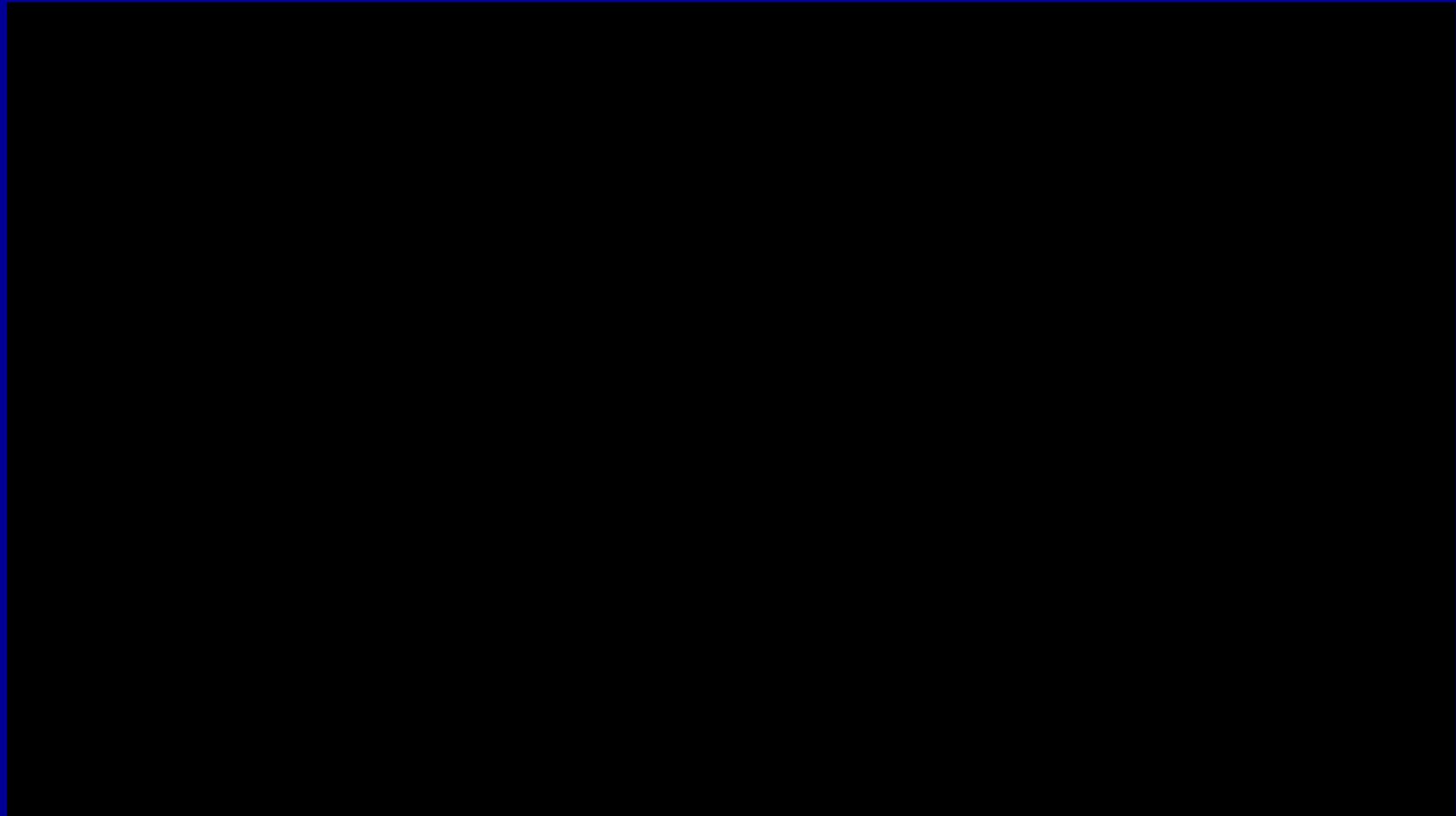


# Gravity wave detectors



GEO600 was not operating on Sept. 15 2015

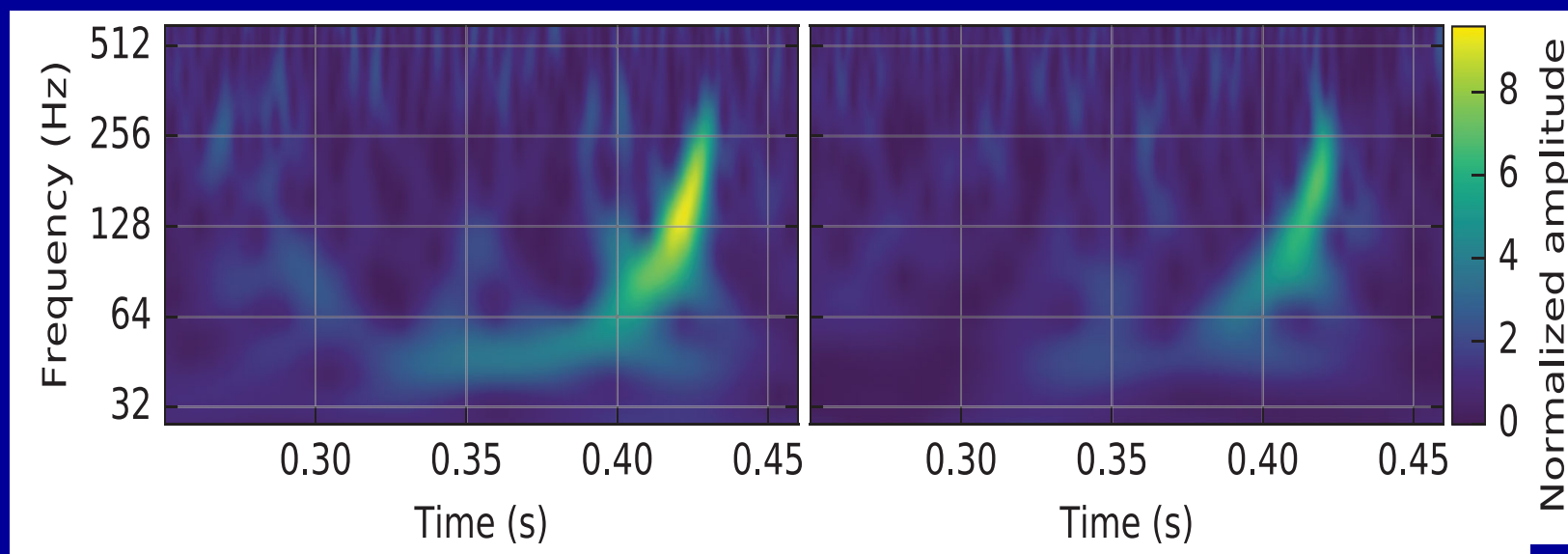
# What are gravitational waves



# The sound chirp

The sound ends around middle C for those of you who know your piano.

Started about G, two and a half octaves lower.



# Mass ranges

- We use the Sun's mass as a unit for studying stars
- We designate it as  $M_o$ ; we say the mass of our sun is  $M_{\text{sun}} = 1 M_o$
- $M_{\text{dwarf}} < 1.39 M_o \Rightarrow$  white dwarf
- $1.39 M_o < M_{\text{ns}} < 3.2 M_o \Rightarrow$  neutron star
- $M_{\text{BH}} > 3.2 M_o \Rightarrow$  black hole
  - stellar sized black holes
  - The original stars lose blow off a lot of mass in their explosions
- Black hole at the center of our galaxy  $M = 10^6 M_o$
- Supermassive Black holes  $10^9 M_o$



# Coalescing black holes

**3.26 x Mpc = Mly: all are in our local supercluster**

Event	$m_1/M_\odot$	$m_2/M_\odot$	$d_L/\text{Mpc}$	$\chi_{\text{eff}}$	$M_f/M_\odot$
GW150914	$35.6^{+4.8}_{-3.0}$	$30.6^{+3.0}_{-4.4}$	$430^{+150}_{-170}$	$-0.01^{+0.12}_{-0.13}$	$63.1^{+3.3}_{-3.0}$
GW151012	$23.3^{+14.0}_{-5.5}$	$13.6^{+4.1}_{-4.8}$	$1060^{+540}_{-480}$	$0.04^{+0.28}_{-0.19}$	$35.7^{+9.9}_{-3.8}$
GW151226	$13.7^{+8.8}_{-3.2}$	$7.7^{+2.2}_{-2.6}$	$440^{+180}_{-190}$	$0.18^{+0.20}_{-0.12}$	$20.5^{+6.4}_{-1.5}$
GW170104	$31.0^{+7.2}_{-5.6}$	$20.1^{+4.9}_{-4.5}$	$960^{+430}_{-410}$	$-0.04^{+0.17}_{-0.20}$	$49.1^{+5.2}_{-3.9}$
GW170608	$10.9^{+5.3}_{-1.7}$	$7.6^{+1.3}_{-2.1}$	$320^{+120}_{-110}$	$0.03^{+0.19}_{-0.07}$	$17.8^{+3.2}_{-0.7}$
GW170729	$50.6^{+16.6}_{-10.2}$	$34.3^{+9.1}_{-10.1}$	$2750^{+1350}_{-1320}$	$0.36^{+0.21}_{-0.25}$	$80.3^{+14.6}_{-10.2}$
GW170809	$35.2^{+8.3}_{-6.0}$	$23.8^{+5.2}_{-5.1}$	$990^{+320}_{-380}$	$0.07^{+0.16}_{-0.16}$	$56.4^{+5.2}_{-3.7}$
GW170814	$30.7^{+5.7}_{-3.0}$	$25.3^{+2.9}_{-4.1}$	$580^{+160}_{-210}$	$0.07^{+0.12}_{-0.11}$	$53.4^{+3.2}_{-2.4}$
GW170817	$1.46^{+0.12}_{-0.10}$	$1.27^{+0.09}_{-0.09}$	$40^{+10}_{-10}$	$0.00^{+0.02}_{-0.01}$	$\leq 2.8$
GW170818	$35.5^{+7.5}_{-4.7}$	$26.8^{+4.3}_{-5.2}$	$1020^{+430}_{-360}$	$-0.09^{+0.18}_{-0.21}$	$59.8^{+4.8}_{-3.8}$
GW170823	$39.6^{+10.0}_{-6.6}$	$29.4^{+6.3}_{-7.1}$	$1850^{+840}_{-840}$	$0.08^{+0.20}_{-0.22}$	$65.6^{+9.4}_{-6.6}$

**Dist/Bly**

**1.4 B ly**

**3.4 B ly**

**1.43 B ly**

**3.1 B ly**

**1.0 B ly**

**9.0 B ly**

**3.2 B ly**

**1.9 B ly**

**0.13 B ly**

**3.3 B ly**

**6.0 B ly**

# The major players in LIGO

**Nobel Prize 2018**



Kip Thorne, Caltech



Rainer Weiss, MIT

**Laser Interferometer Gravitational-Wave Observatory (LIGO)**

is a large-scale, very high-precision, physics experiment and observatory to detect gravitational waves. Sponsored by NSF.



# Arms are 4 km long

They want to detect  $h = \Delta L/L = 10^{-22}$

The laser travels 8 km, so  $L = 8 \times 10^3$  m

$$\Delta L = 10^{-22} \times 8 \times 10^3 \text{ m} = 8 \times 10^{-19} \text{ m}$$

$$\Delta L = 8 \times 10^{-17} \text{ cm}$$

**Size of proton  $1.6 \times 10^{-13}$  cm**

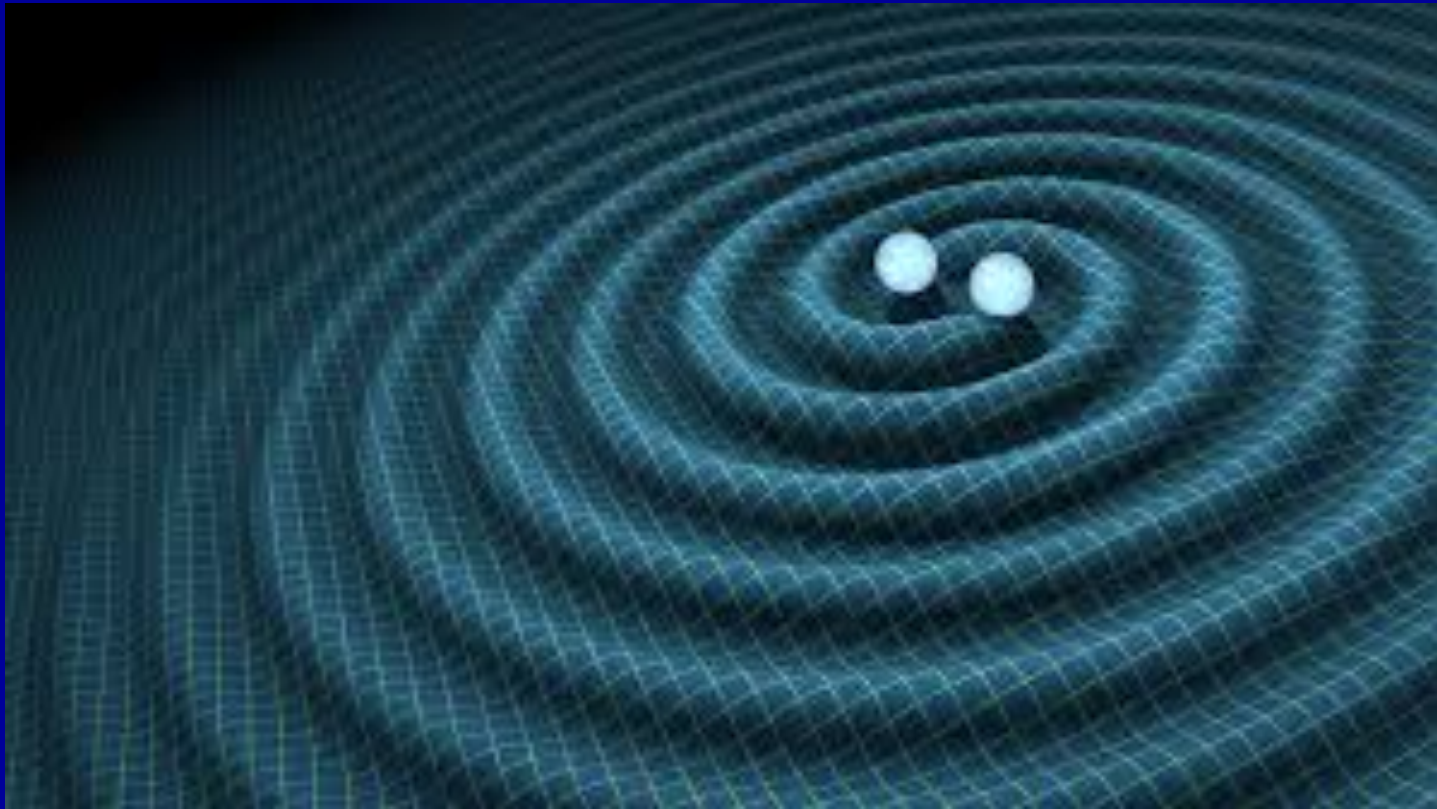
# How big is $10^{-17}$ cm?

An amazing technical 'tour de force'!!

- So  $10^{-17}$  cm is two thousandth of the size of a proton. The motion detected was one tenth of a millionth of a billionth of a millimeter.
  - If you compare this and put the number into dollars, with a millimeter being like a dollar, it is like having 2 thousand trillion dollars or something like 20 times the size of our national debt.

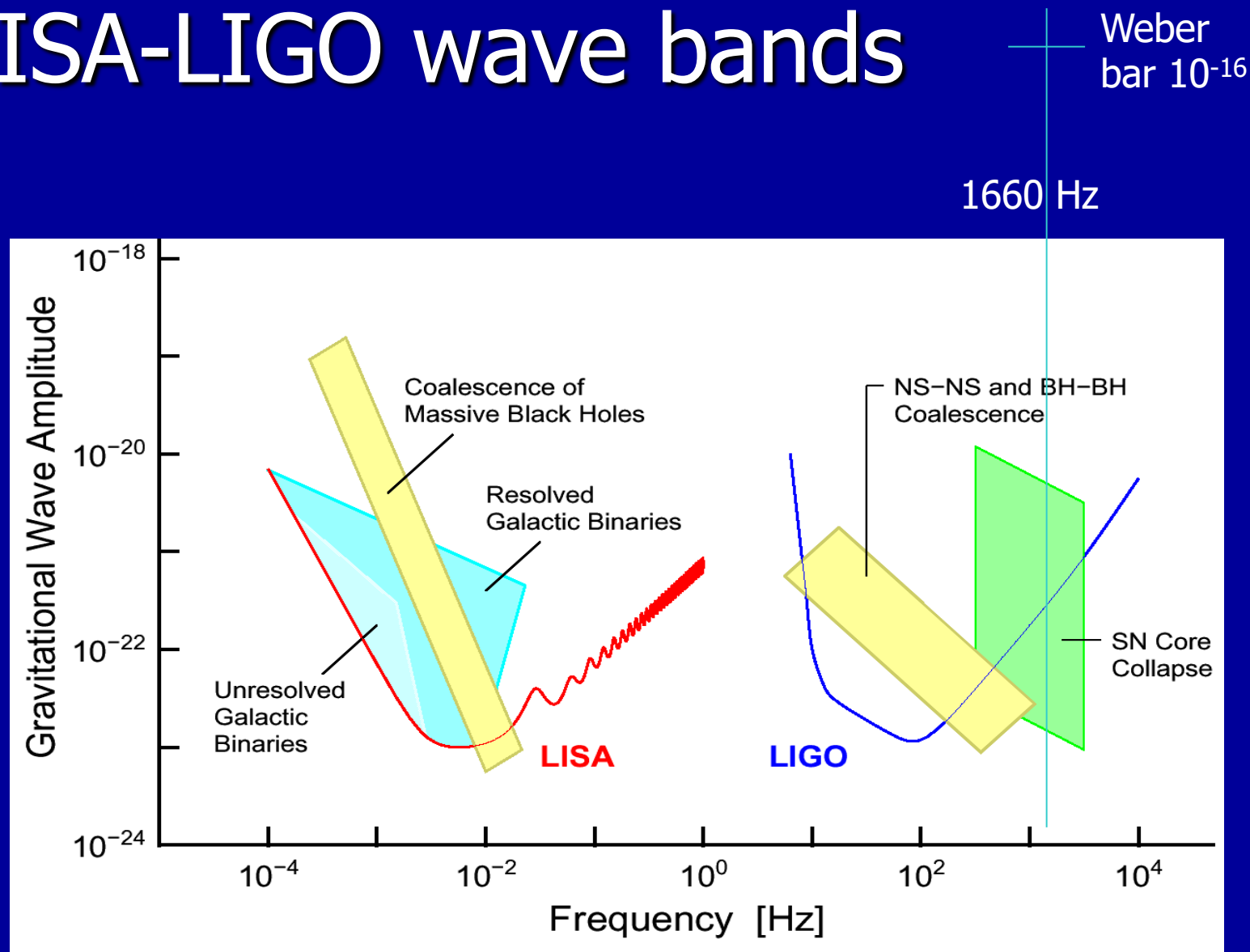
Stop here

36  $M_{\odot}$  and 29  $M_{\odot}$   $\rightarrow$  62  $M_{\odot}$  ( $\pm 4 M_{\odot}$ )  
distance 1.3 billion light years  
Note: 36  $M_{\odot}$  + 29  $M_{\odot}$  = 65  $M_{\odot}$   
3  $M_{\odot}c^2$  energy in gravitational waves



Sept 14, 2015 during the aLIGO calibration run

# LISA-LIGO wave bands



# An outstanding paper

PRL **116**, 061102 (2016)

 Selected for a [Viewpoint](#) in *Physics*  
PHYSICAL REVIEW LETTERS

week ending  
12 FEBRUARY 2016



## Observation of Gravitational Waves from a Binary Black Hole Merger

B. P. Abbott *et al.*\*

(LIGO Scientific Collaboration and Virgo Collaboration)

(Received 21 January 2016; published 11 February 2016)

Primary black hole mass	$36^{+5}_{-4} M_{\odot}$
Secondary black hole mass	$29^{+4}_{-4} M_{\odot}$
Final black hole mass	$62^{+4}_{-4} M_{\odot}$
Final black hole spin	$0.67^{+0.05}_{-0.07}$
Luminosity distance	$410^{+160}_{-180} \text{ Mpc}$
Source redshift $z$	$0.09^{+0.03}_{-0.04}$

# Conclusions

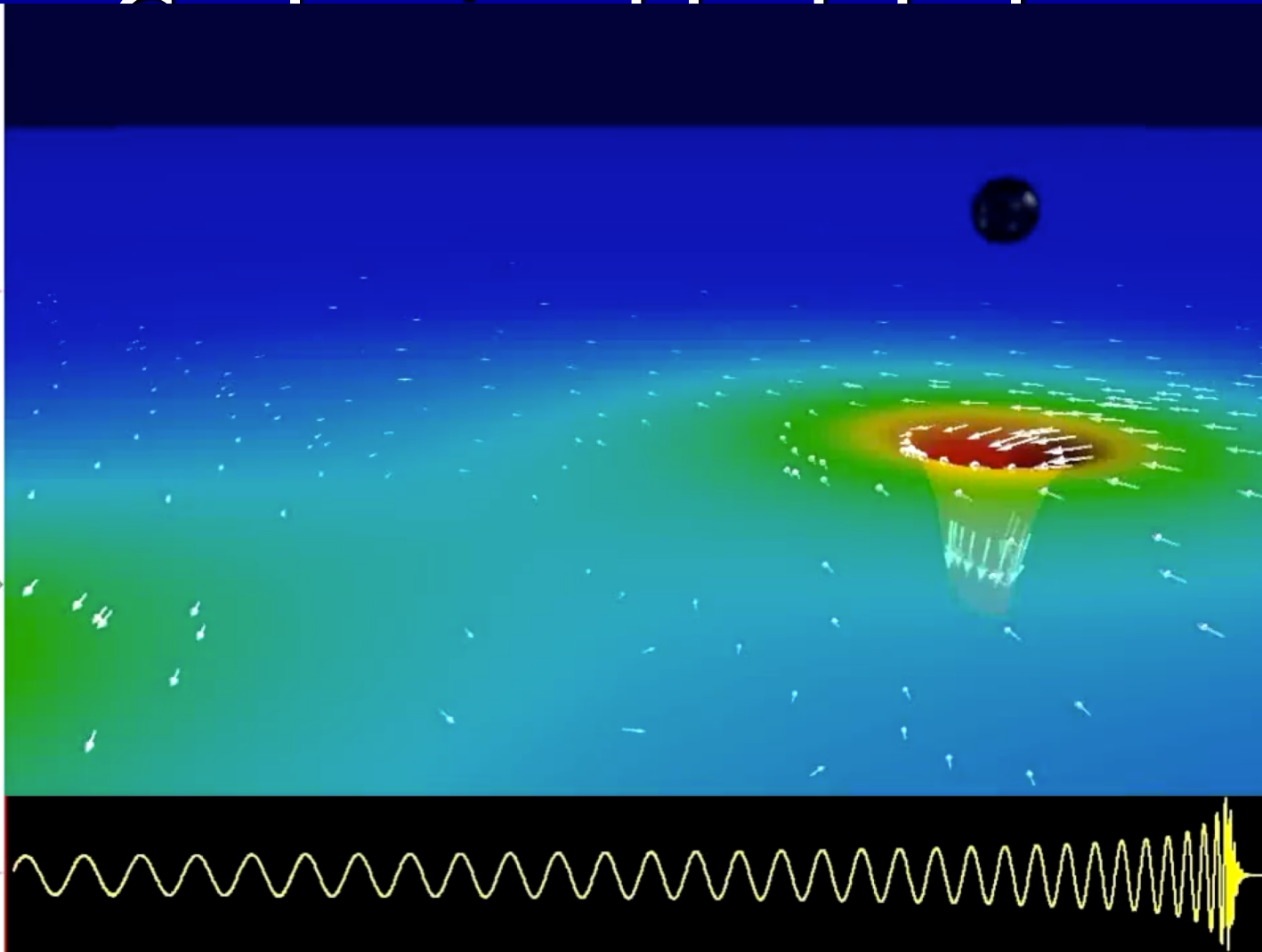
- Observations demonstrate that gravitational waves travel at the speed of light and that gravity has no mass, as predicted by Einstein's general relativity.
- We can now estimate the rate at which Black hole coalescences are taking place in the nearby (100 M ly).

## Black Hole Evolution: Computer Simulation

View of Black Holes  
and Trajectory

Spacetime curvature:  
curvature of space  
rate of flow of time  
density of flow of space

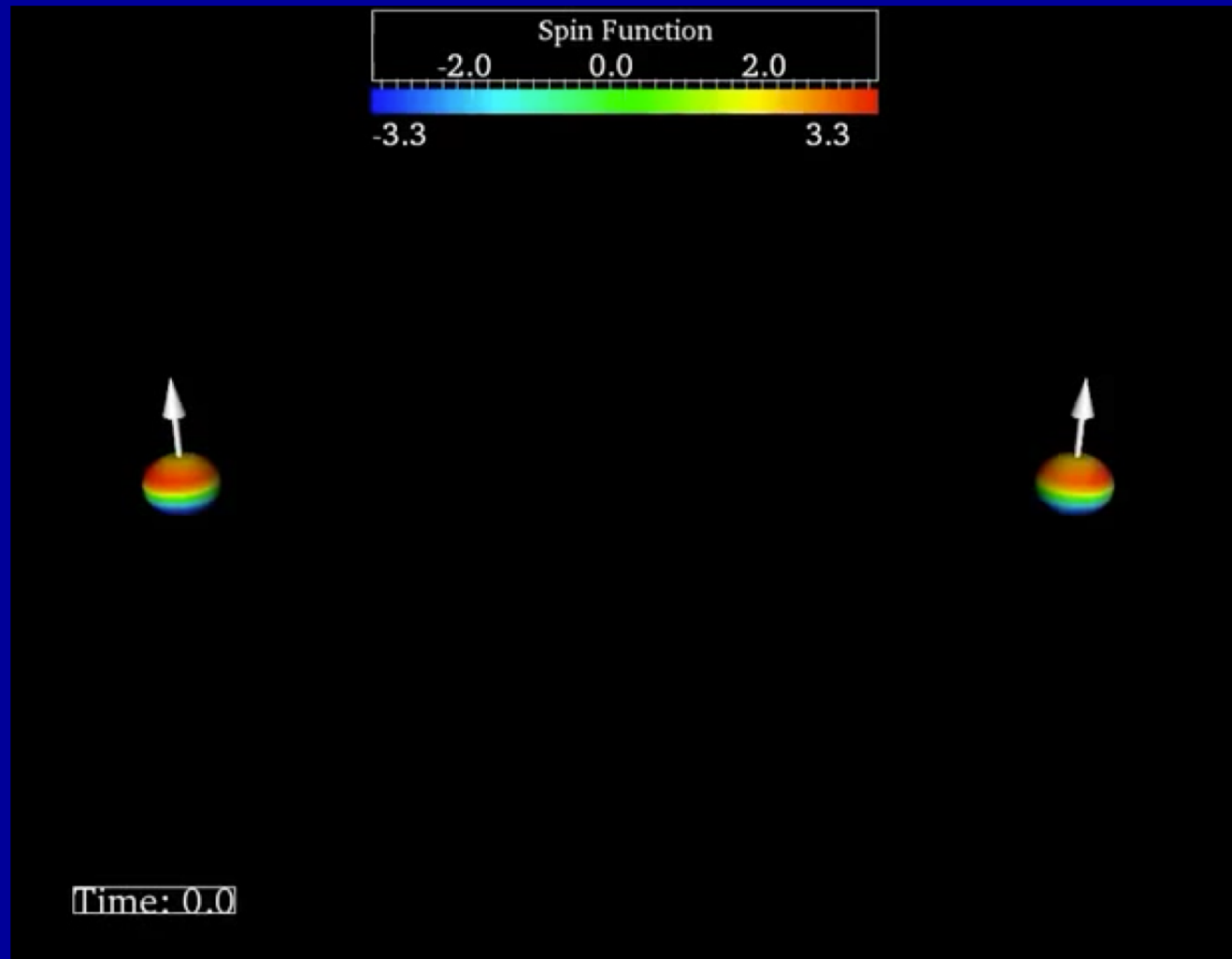
Gravitational waveform  
(vs current time)



[https://www.youtube.com/watch?v=L478ZPy\\_2Ys](https://www.youtube.com/watch?v=L478ZPy_2Ys)



# Coalescing black hole simulations



# GW170817

Discovered by LIGO and Virgo Observatories  
Chirp 100 sec by LIGP

1.7 s later by Fermi and INTEGRAL – gamma-rays

11 hours later optical counterpart

Observed from radio to X-rays -> kilonova

another similar event found without GW counterpart

Swift, Chandra and 70 other observatories

Jet outflows probably not directed towards Earth

Region now neutron rich

Paper with 4000 authors (2/3 of world's astronomers)

Distance 40 Mpc

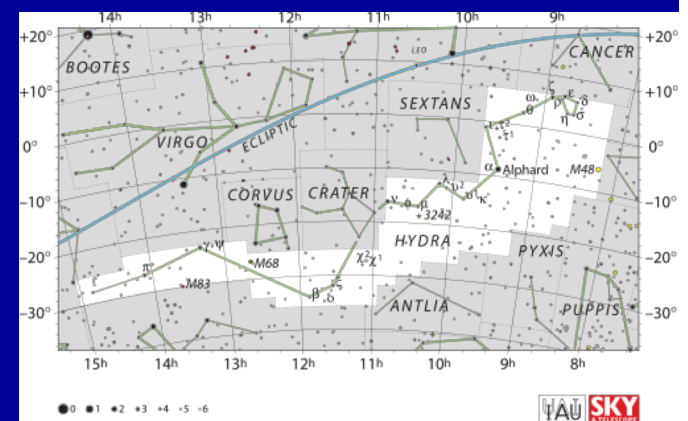
2 kpc from center of NGC4993 in constellation Hydra

Binary neutron star system

Gravitational waves when they coalesced

$M_1$  in the range  $1.36\text{--}2.26 M_\odot$

$M_2$  in the range  $0.86\text{--}1.36 M_\odot$



Such events  
produce the  
elements heavier  
than iron – called  
r-process nuclei



# Amplitudes of Gravitational Wave Sources . . .

- Strongest sources have large masses moving with  $v \sim c$

Characteristic GW amplitude  $h$

Estimated upper limits (circa 2003):

- $10 M_{\odot}$  Black Hole at
  - $r = 50,000$  light-years,  $h \sim 10^{-16}$
  - $r = 50$  million light-years,  $h \sim 10^{-19}$
  - $r = 650$  million light-years,  $h \sim 10^{-20}$
  - $r = 10$  billion light-years,  $h \sim 10^{-21}$
- $2.5 \times 10^6 M_{\odot}$  Massive Black Hole at
  - $r = 10$  billion light-years,  $h \sim 10^{-16}$